

Once, to never forget, the derivation. Given a point  $x_i$  called the *initial estimate*, and a function  $f(x)$ , we can make an approximation  $x_u$  for  $x_0$  s.t.  $f(x_0) = 0$  by constructing the 1-st order approximation to  $f$  at  $x_i$ . The equation of this line, translated to  $t = x - x_i$  is

$$l(t) = f(x_i) + tf'(x_i).$$

Solving for  $t_u$  s.t.  $l(t_u) = 0$  gives  $t_u = -f(x_i)/f'(x_i)$ , or

$$x_u = u(x_i) = x_i - \frac{f(x_i)}{f'(x_i)}.$$

The function  $u$  can now be iteratively applied to refine the estimate.