

A differential of a function on a manifold $f :: M \rightarrow \mathcal{R}$ is a linear functional $df_p(t) :: T_p \rightarrow \mathcal{R}$ defined on the tangent space T_p at $p \in M$.